2008 VCAA Further Mathematics Exam 1 Solutions Free download and print from www.itute.com Do not photocopy © Copyright 2008 itute.com

SEC	TIO	NΑ	Co	ore: l	Data	anal	ysis					
1	2	3	4	5	6	7	8	9	10	11	12	13
D	Е	В	Α	С	В	D	С	С	Е	Е	С	D

SECTION B

SECT	SECTION D								
Module 1: Number patterns and applications									
1	2	3	4	5	6	7	8	9	
Е	D	В	Е	В	D	Α	D	D	
Modul	Module 2: Geometry and trigonometry								
1	2	3	4	5	6	7	8	9	
В	D	D	Α	Α	D	Α	Е	D	
Modul	Module 3: Graphs and relations								
1	2	3	4	5	6	7	8	9	
В	A	С	С	В	D	С	D	A	
Modul	Module 4: Business-related mathematics								
1	2	3	4	5	6	7	8	9	
Е	D	В	С	В	A	В	В	C	
Modul	Module 5: Networks and decision mathematics								

1	2	3	4	5	6	7	8	9
C	В	Α	В	Е	D	C	C	Α
Module 6: Matrices								
1	2	3	4	5	6	7	8	9

Module 6: Matrices									
	1	2	3	4	5	6	7	8	9
	D	Е	С	В	Е	В	Α	D	D

SECTION A Core: Data analysis

Q1	Read from box plot.	Γ)

Q3
$$25\% \times 79 = 19.75$$
 B

Q4 For positively skewed distribution the mean is greater than the median. A

Q5 Data: 0 0 0 1 1 2 2 2 2 3 3 4 4 5
Use graphics calc. to find
$$\bar{x} = 2.1$$
, $s = 1.6$.

Q7 2.5% is lower than
$$\mu - 2\sigma$$
, 16% is greater than $\mu + \sigma$. Total 18.5%

Centring:
$$\frac{359 + 361.5}{2} = 360.25$$

Q13 December 2009 is the
$$36^{th}$$
 month.
Number of users = $346 + 2.77 \times 36 = 445.72$

SECTION B

Module 1: Number patterns and applications

Q1 2 times the previous number + 1 to get the next number.

$$2 \times 15 + 1 = 31$$

$$O2 8600 - 25 \times 60 = 7100$$

E

D

D

Q3 Read from graph, a = 100. The terms alternate between + and -, \therefore r is a negative value. r = -0.9 to get the second term.

Q4 Geometric sequence:
$$a = B_0 = 800$$
, $r = 1 + \frac{15}{100} = 1.15$. E

O5 Geometric sequence: 9, x, 121.

$$r = \frac{x}{9} = \frac{121}{r}$$
, $x^2 = 9 \times 121$, $x = -33$ or 33.

Q6 The sequence 15, 19, 23, 27 is arithmetic. a = 15, d = 4,

$$S_{12} = \frac{12}{2} (2 \times 15 + (12 - 1)4) = 444$$
.

O7
$$12+15=27$$
, $15+27=42$ etc.

Q8 The length increases form a geometric sequence with a = 3.6 and r = 0.75.

The maximum total increase =
$$\frac{a}{1-r} = \frac{3.6}{0.25} = 14.4$$

The maximum length = $14.2 + 14.4 = 28.6$

Q9
$$T_1 = 0.98 \times 50000 + 500 = 49500$$

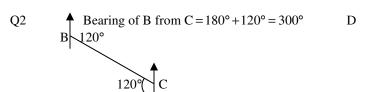
$$T_2 = 0.98 \times 49500 + 500 = 49010$$

$$T_3 = 0.98 \times 49010 + 500 = 48529.8$$

$$T_4 = 0.98 \times 48529.8 + 500 = 48059.204$$

Module 2: Geometry and trigonometry

Q1
$$a = 180 - 73 - 73 = 34$$
 B



Q3
$$s = \frac{7.0 + 8.0 + 12.3}{2} = 13.65$$

$$A = \sqrt{13.65(13.65 - 7.0)(13.65 - 8.0)(13.65 - 12.3)} \approx 26.3$$

Q4
$$V = \pi r^2 h$$
, $490.87 = \pi r^2 \times 25.15$, $r \approx 2.5$

Q5 The sine rule:
$$\frac{\sin x^{\circ}}{4} = \frac{\sin 125.1^{\circ}}{8}$$
, $\sin x^{\circ} = \frac{\sin 125.1^{\circ}}{2}$.

Q6 Total = base + 2 semicircles + curved surface

=
$$(1.5)(2.5) + 2 \times \frac{1}{2} \pi (0.75^2) + \pi (0.75)(2.5) \approx 11.4$$

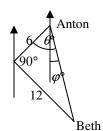
Q7
$$V = \frac{1}{3}\pi r^2 h = \frac{1}{3}\pi (1.3^2)(1.2) \approx 2.1$$

Q8 Use the centre to divide the hexagon into 6 congruent triangles (base = 3.0, height = 2.6).

$$A = 6\left(\frac{1}{2} \times 3.0 \times 2.6\right) = 23.4$$

Q9
$$\theta = \tan^{-1} \left(\frac{12}{6} \right) = 63.43$$
, $\varphi = 63.43 - 45 = 18.43$

Bearing =
$$180 - 18.43 \approx 162^{\circ}$$



Module 3: Graphs and relations

- Q1 Read from graph.
- Q2 2t litres flow out after t minutes. V = 5000 2t
- Q3 The graph is not linear.
- Q4 Monday at Easypark, Tuesday at Safepark:

$$8 + 2.50 \times 3 = $15.50$$

Q5
$$2x + 3y = 12$$

$$y = 4$$
 when $x = 0$ and $x = 6$ when $y = 0$

Q6 4d + 6b = 14.70 and 3d + 5b = 11.90.

Solve to find d = 1.05 and b = 1.75.

$$\therefore 1d + 2b = \$4.55$$

Q7 Gradient of y vs
$$x^2$$
 graph is $\frac{1}{4}$. $\therefore y = \frac{1}{4}x^2$.

D

Α

A

D

 \mathbf{C}

В

Q9 The gradient of the objective function must be between the gradients of the two given lines, -2.5 and -0.5.

$$Z = x + y$$
 has a gradient of -1 .

D

В

Module 4: Business-related mathematics

Q1 Full price =
$$300 + 300 \times 0.10 = $330$$
 E

D Q2
$$Q = \frac{\text{Pr}}{100n} = \frac{800000 \times 5.8}{100 \times 26} \approx 1785$$
 D

Q3
$$V = P \left(1 - \frac{r}{100} \right)^t$$
, $2000 = 6000 \left(1 - \frac{r}{100} \right)^4$

$$1 - \frac{r}{100} = 0.75984$$
, $r \approx 24$

E Q4 4200-600=3600, interest = $0.06\times3600=216$.

Total repayment = 3600 + 216 = 3816

Monthly instalment =
$$\frac{3816}{12}$$
 = \$318

Q5 Effective rate =
$$\frac{100I}{Pt} \times \frac{2n}{n+1} = \frac{100 \times 216}{3600 \times 1} \times \frac{2 \times 12}{12+1} \approx 11.1$$
 B

Q6 Sam:
$$A = 5000 + \frac{5000 \times 7.5 \times 3}{100} = $6125$$

Charlie:
$$A = 5000 \times 1.075^3 = \$6211.48$$

Difference = $6211.48 - 6125 = \$86.48$

Q7 The rate at which the amount paying off the principal increases over the period because of the effect of reducing balance.

B Q8 Use TVM Solver:
$$N = 80$$
, $PV = 300000$,

A
$$PMT = -6727.80$$
, $FV = 0$, $F/Y = 4$, $C/Y = 4$, $PMT : END$ to obtain $I\% = 6.500001746$

Q9
$$P = 8000$$
, $R = 1 + \frac{7.2}{100 \times 4} = 1.018$

Module 5: Networks and decision mathematics

Q4

Q5 The addition of one further edge, e.g. connecting C and D,

will result in only 2 odd-degree vertices.

Ε

В

Q6 6+6+8+9+7+2+4=42

D

Q7 v+f-e=2, 5+f-9=2, f=6

C

Q8

C

Q9

A

Module 6: Matrices

Q1 1+d=11, d=10

D

Q2

E

Q3

C

Q4

В

Q5 $3x-2\times6=9$, x=7

Ε

Q6 Use graphics calculator:

$$\begin{bmatrix} 0 & -3 & 2 \\ 1 & 1 & 1 \\ -2 & 0 & 3 \end{bmatrix}^{-1} \begin{bmatrix} 11 \\ 5 \\ 8 \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \\ 4 \end{bmatrix}$$

В

Q7 20% of 2800 = 560

A

Q8
$$T^{100} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ \frac{3}{4} & 1 & \frac{2}{3} & 0 \\ 0 & 0 & 0 & 0 \\ \frac{1}{4} & 0 & \frac{1}{3} & 1 \end{bmatrix}$$

D

Q9
$$\begin{bmatrix} 0.35 & 1 & 0.15 & 0 \\ x \\ x \\ x \end{bmatrix} \begin{bmatrix} x \\ x \\ x \end{bmatrix} = \begin{bmatrix} 6000 \\ 0 \\ 0 \end{bmatrix}$$

 $\therefore 0.35x + x + 0.15x = 6000$, $\therefore x = 4000$, 4x = 16000.

D

Please inform mathline@itute.com re conceptual, mathematical and/or typing errors